

7.2 - Inverse Transforms and Transforms of Derivatives

Theorem 7.2.1: Some Inverse Transforms

$$(a) 1 = \mathcal{L}^{-1} \left\{ \frac{1}{s} \right\}$$

$$(b) t^n = \mathcal{L}^{-1} \left\{ \frac{n!}{s^{n+1}} \right\}, n = 1, 2, 3, \dots$$

$$(c) e^{at} = \mathcal{L}^{-1} \left\{ \frac{1}{s-a} \right\}$$

$$(d) \sin kt = \mathcal{L}^{-1} \left\{ \frac{k}{s^2 + k^2} \right\}$$

$$(e) \cos kt = \mathcal{L}^{-1} \left\{ \frac{s}{s^2 + k^2} \right\}$$

$$(f) \sinh kt = \mathcal{L}^{-1} \left\{ \frac{k}{s^2 - k^2} \right\}$$

$$(g) \cosh kt = \mathcal{L}^{-1} \left\{ \frac{s}{s^2 - k^2} \right\}$$

Example: Find the inverse Laplace transform.

$$\mathcal{L}^{-1} \left\{ \frac{1}{s^4} \right\}$$

$$\mathcal{L}^{-1} \left\{ \frac{10s}{s^2+16} \right\}$$

$$\mathcal{L}^{-1} \left\{ \frac{s+1}{s^2+2} \right\}$$

$$\mathcal{L}^{-1} \left\{ \frac{s+1}{s^2-4s} \right\}$$

Example: Use the Laplace transform to solve the Initial-Value Problem.

$$2 \frac{dy}{dt} + y = 0, \quad y(0) = -3$$

Transforms of derivatives



